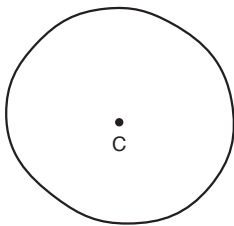


APPENDIX 1

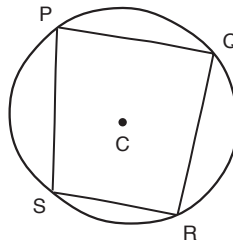
Item G1 (right) was used in the Year 8 and Year 10 proof tests for the Longitudinal Proof Project. We discuss the item in chapter 8 (page 8.4).

On this page (below) we show selected 'Yes' responses to the item; on the next page we show selected 'No' responses. The responses can be used with students to help them develop an awareness of the different qualities of students' written explanations (see chapter 7).

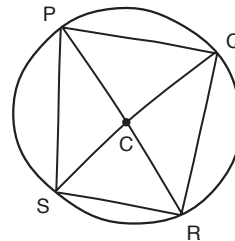
Darren sketches a circle. He calls the centre C.



He then draws a quadrilateral PQRS, whose corners lie on the circle.



He then draws the diagonals of the quadrilateral.



Darren says

"Whatever quadrilateral I draw with corners on a circle, the diagonals will always cross at the centre of the circle".

Is Darren right?

.....

Explain your answer.

Is Darren right? ...Yes...

Explain your answer.

Because all quadrilaterals have 4 sides the diagonals always have to go from one side of the circle to the opposite side, so the diagonals always have to go through ~~the~~ the centre.

A

Is Darren right? ...Yes...

Explain your answer.

The quadrilaterals corners are on the edges of a circle so they will have the same centre point as the quadrilateral.

C

Is Darren right? ...Yes

Explain your answer.

Because one diagonal going across the circle is like the diameter.

B

Is Darren right? ...Yes...

Explain your answer.

Because whatever way you look at the shape the corners are always going to be in line with the centre.

D

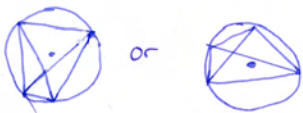
APPENDIX 1, continued

Selected 'No' responses to item G1:

Is Darren right? ..No....

Explain your answer.

It depends where the corners of the quadrilateral lie. If they are not ~~completely~~ opposite one another the diagonals will miss the centre of the circle.
e.g.



or

E

Is Darren right? ..No....

Explain your answer.

because a quadrilateral is a shape with 4 sides but it doesn't mean they have to be equal.

H

Is Darren right? ..No....

Explain your answer.

If the ^{opposite} corners aren't opposite each other the diagonals will not intersect ~~on the circle~~ at the centre of the circle.

F

Is Darren right? ..No....

Explain your answer.

The corners could all be above or below the center, taking up less than half of the circle

I

Is Darren right? No
~~Yes~~....

Explain your answer.

Because all the corners can touch above the centre of the circle
e.g.



G

APPENDIX 2

Item G2b (right) was used in all three proof tests for the Longitudinal Proof Project. We discuss the item in chapter 8 (page 8.5).

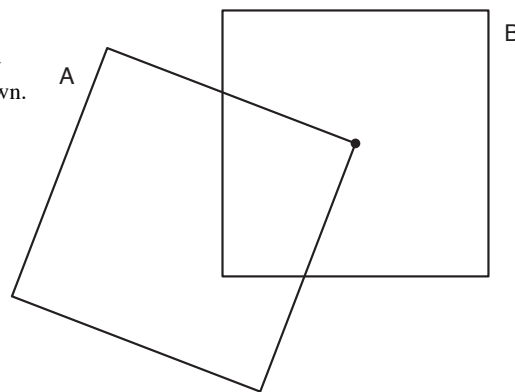
On this page (below) and the next, we show selected responses to the item. The responses can be used with students to help them develop an awareness of the different qualities of students' written explanations (see chapter 7).

One corner of tile A is moved to the centre of tile B, as shown.

What fraction of tile B is overlapped by tile A ?

.....

Explain your answer.



One corner of tile A is moved to the centre of tile B, as shown.

What fraction of tile B is overlapped by tile A ?

...1/4...

Explain your answer.

If you turned the overlapping square round so that the sides are parallel to the other square it will be clear that a quarter is overlapping.

G2bCM01

One corner of tile A is moved to the centre of tile B, as shown.

What fraction of tile B is overlapped by tile A ?

...1/4...

Explain your answer.

A, B, C, D are all equal.
There are 4 of them so they must be quarters.

G2bGH30

One corner of tile A is moved to the centre of tile B, as shown.

What fraction of tile B is overlapped by tile A ?

...1/4...

Explain your answer.

Because the corner of the square is a right angle (90°) and so a 90° angle is overlapped which is a quarter. (1/4)

G2bPC01

One corner of tile A is moved to the centre of tile B, as shown.

What fraction of tile B is overlapped by tile A ?

...1/4...

Explain your answer.

Because if you line the squares up like this (the square A being rotated) then it covers 1/4 because the corner of A is exactly in the centre of B. Therefore, no matter where A moves, so long as 1 corner is in the centre of B, it will always cover 1/4

G2bJC30

APPENDIX 2, continued

More responses for item G2b:

One corner of tile A is moved to the centre of tile B, as shown.

What fraction of tile B is overlapped by tile A?

$\frac{1}{4}$

Explain your answer.

It must be overlapping a $\frac{1}{4}$ of A because it goes from the centre so only one quarter of the tile can possibly overlap.

G2bC20Y8AM05

E

One corner of tile A is moved to the centre of tile B, as shown.

What fraction of tile B is overlapped by tile A?

$\frac{1}{4}$

Explain your answer.

The two lines go straight to the centre. we can see the shape made would roughly fill the tile 4 times

G2bSM01

H

One corner of tile A is moved to the centre of tile B, as shown.

What fraction of tile B is overlapped by tile A?

$\frac{1}{4}$

Explain your answer.

This is because the fully shaded area has been moved to the non full area that is shaded. so the area stays the same and so does the side.

G2bSA01

F

One corner of tile A is moved to the centre of tile B, as shown.

What fraction of tile B is overlapped by tile A?

$\frac{1}{4}$

Explain your answer.

Because if you moved the tile slightly you would be able to see more clearly that $\frac{1}{4}$ of the tile is being overlapped.

G2bSP01

I

One corner of tile A is moved to the centre of tile B, as shown.

What fraction of tile B is overlapped by tile A?

$\frac{1}{4}$

Explain your answer.

Because the an angle of the corner is 90° & is coming from the centre of square and 90° which is 360° and $\frac{90}{360} = \frac{1}{4}$

G2bSM01

G

One corner of tile A is moved to the centre of tile B, as shown.

What fraction of tile B is overlapped by tile A?

$\frac{1}{4}$

Explain your answer.

$\frac{1}{4}$

G2bY8c31RB26

J

APPENDIX 3

Question A4 was used in the Year 8 and Year 9 proof tests for the Longitudinal Proof Project. In part c) students are asked whether $100!$ is divisible by 31 (Year 8) or whether $50!$ is divisible by 19 (Year 9). We discuss the item in chapter 8 (page 8.5).

Selected responses to item A4c are shown below. The responses can be used with students to help them develop an awareness of the different qualities of students' written explanations (see chapter 7).

Is $50!$ exactly divisible by 19? ...Yes...

Explain your answer.

the number has been multiplied by 19, so it must be divisible by 19

A4cC40Y9AM24 A

Is $100!$ exactly divisible by 31? ...NO...

Explain your answer.

$5 = 120$

$5 \ 10$
 20

$\begin{array}{r} 120 \\ \times 20 \\ \hline 2400 \end{array}$

A4cC12Y8KM07 D

Is $100!$ exactly divisible by 31? ...No...

Explain your answer.

~~100! = 31 x 28 x 28~~

~~100 = 31 x 3~~

31 is a prime number and can't be divided into anything

A4cC93Y8BJ11 B

Is $100!$ exactly divisible by 31? ...No...

Explain your answer.

Because at $5!$ the answer is 120 which has a zero at the end and so you won't get anything in that column from now on and

(eg. $90 \div 31$
 $100 \div 31$
 $110 \div 31$) don't equal a whole number

A4cC93Y8NB64 E

Is $100!$ exactly divisible by 31? ...No...

Explain your answer.

This is because 31 is an odd number and the end result of $100!$ is an even number.

A4cC93Y8GI09 C

Is $50!$ exactly divisible by 19? ...Yes...

Explain your answer.

Factorial is when any number is it can be divisible in the final number.

$4 \times 3 \times 2 \times 1 = 24$, 4, 3, 2, and 1 can all fit into 24.

So 19 does go into $50!$, so will be in the answer.

A4cC20Y9MC07 F

